Safe and Chaotic Compilation for Hidden Deterministic Hardware Aliasing

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REG PAPER

Abstract—Hardware aliasing occurs when the same logical address can access different physical memory locations. This is a problem for software on some embedded systems and more generally when hardware becomes faulty in irretrievable locations, such as on a Mars Lander. We show how to work around the hardware problem with software logic, compiling code so it works on any platform with hardware aliasing with hidden determinism. That is: (i) a copy of an address accesses the same location, and (ii) repeating an address calculation exactly will repeat the same access again. Stuck bits can mean that even adding zero to an address can make a difference in that environment so nothing but a systematic approach has a chance of working. The technique is extended to generate aliasing as well as compensate for it, in so-called chaotic compilation, and a sketch proof is included to show it may produce object code that is secure against discovery of the programmer’s intention. A prototype compiler implementing the technology covers all of ANSI C except long jmp/set jmp.

I. INTRODUCTION

Hardware aliasing describes “the situation where, due to either a hardware design choice or a hardware failure, one or more of the available address bits is not used in the memory selection process.” [1] The effect used to be familiar to programmers and users alike, as the ‘DOS hell’ that the old 16-bit versions of Windows were prone to. Dynamic linked libraries (DLLs) were problematic for many reasons, but one was that different versions of the same library loaded at the same memory address and all applications referenced the in-memory copy. So if one application loaded one version of the library then another loaded another version, the first application would unpredictably, as far as the program and user were concerned, find itself in the second library’s code.

DOS users truly experienced the situation in the raw, as the ubiquitous expanded memory managers (for memory beyond 1MB) such as QuarterDeck’s QEMM [2] remapped memory so the video graphics (VGA) and bootstrap (BIOS) code shared addresses with random access memory (RAM). What a program accessed at runtime at a given address depended on the memory manager heuristics. In consequence, code had to use standard sequences to trigger expanded memory reliably. Nowadays, processors such as the Raspberry PI-2 (all models) [3] still dynamically share up to 1GB of RAM for general-purpose use with the graphics processing unit (GPU).

Whatever the physical rationale, the symptom is the same in every case. It is that what looks to programs to be the same memory address (the logical address) sporadically accesses physically different resources. Since the memory management hardware in modern processors maps all input/output (I/O) into one monolithic processor address space, that may mean different regions of RAM or it may mean different peripheral devices such as USB (‘universal serial bus’) and GPU.

Certainly, modern applications programmers are more familiar with software aliasing, in which the same physical resource—memory location or peripheral device—is accessible via different logical addresses. But hardware aliasing has not gone away so much as become less relevant for the ordinary programmer as platforms have evolved to present a normalised view to software. The paradigm of platform hardware that actually has hardware aliasing through and through but presents ‘normally’ to even a systems programmer is oblivious RAM (ORAM) [4], [5], [6]. That is a secure RAM solution (available in various forms since the 90s) in which internally the memory contents are continuously randomly aliased and re-aliased to frustrate cold boot attacks [7] (freezing the RAM sticks to make the electrical charge last longer for analysis; RAM chips require a read-and-rewrite cycle to maintain their contents and ordinarily taking them out of the processor would lose the contents immediately). But the closer the programmer works to hardware the less complete may be the facade. On platforms which are both resource-limited and relatively inaccessible, programmers have to work around not only hardware that shares the same address space but faults that can exacerbate the situation. A stuck bit may take one address line out of commission, forcing the hardware map into a smaller shared address space. Or a Mars Lander may suffer a cosmic ray through the processor that causes the arithmetic logic circuit to compute 1+1=3. One way to cope with that is to rewrite programs to treat 2 and 3 as indistinguishable for the purposes of arithmetic. That means rewriting to work in arithmetic modulo a suitable equivalence. That may be, for example here, a partition of the number space into pairs \{2, 3\}, \{4, 5\}, etc., in which \{2m, 2m+1\}∪\{2n, 2n+1\} = \{2(m+n), 2(m+n)+1\} and \{2m, 2m+1\} ∗ \{2n, 2n+1\} = \{2mn, 2mn+1\}. That equivalence should in general be the least indiscriminatory that makes the processor’s faulty answers x+y into a homomorphic image of standard computer arithmetic.\(^1\) That entails losing one arithmetic bit or more, since the only homomorphic images have sizes that are factors of the original size \(2^n\), which will be \(2^m\) for some \(m < n\).

\(^1\)The simplest construction of a suitable equivalence is to set the processor’s wrong result 1 + 1 = 3 equivalent to the correct result 1 + 1 = 2, with 2 ∩ 3, and then close under the implications \(x_1 \equiv x_2 \wedge y_1 \equiv y_2 \rightarrow x_1 + y_1 \equiv x_2 + y_2\), where the + is the correct one. Similarly for multiplication, etc. The equivalence shown is \(x \equiv y\) iff \(\lfloor x/2 \rfloor = \lfloor y/2 \rfloor\), with 2 ∩ 3.
While 4 and 5 may denote the same value arithmetically, as addresses they access different memory locations and a program rewritten to accommodate a nontrivial arithmetic equivalence will experience hardware aliasing. So the cure for the computational mathematics engenders a need to handle the consequential aliasing. Since low-level programs in particular use pointers heavily, there is no room for an ad hoc approach to that. Even high-level programming languages use pointers nearly ubiquitously – every object in Java is really a pointer, so copying an object requires the clone() system call. A simple copy will just be another pointer to the same object. Every variable in Fortran95 is a pointer – a subroutine call f(x) alters the value of its caller’s variable x when the subroutine writes to x. Arrays in C are passed as pointers too. Not only will system-level programmers need a reliable way to program around hardware aliasing because systems programming is hard enough without new traps for the unwary, but application-level programmers, the mathematicians and control engineers, must be able to remain comfortably ignorant of the hazard.

It turns out that there is a systematic way of generating code that always works in a hardware aliasing environment – a compiler mechanism – and this paper sets it out. There has been no other work on this topic since the present authors made an original suggestion as to what to do in 2014 [8], but experience has shown that suggestion to be too delicate for practice (the reference is anonymised but the idea was to set up different type classes for arrays – in one, array entries are uniquely accessed by walking a pointer in unit increments up from the bottom of the array, in another, access is uniquely by walking down from the top, in another, access is uniquely via a single constant offset from the bottom of the array, and so on; each class enforces a unique calculation for each array entry which produces the same result each time, as discussed below, but the programmer must choose what type to declare each array as and there is no proof that deeply nested arrays of pointers to arrays of pointers, etc., will not give rise to inconsistencies). The technology reported in this paper is less efficient computationally but it is robust and usable in practice by programmers, and it has been deployed and tested – c.f. the HAVOC compiler suite for ANSI C [9] at http://sf.net/p/obfusc.

The programmer is aware only that each pointer must be declared with restrict. That modifier nominates a top-level (or local) memory zone that the pointer is to range through. Not declaring a zone means the compiler assumes the pointer can point anywhere at runtime, which causes prohibitively large object code to be generated – gigabytes for a line of source code – so it behoves the programmer to declare a small zone.

The solution works because of an underlying determinism in processors. Processors are mechanisms that are both designed to produce repeatable results and also do so inherently because of their material. They are quite high power electronic logic circuits, which makes it rare for a faulty bit to be really random. Even if the electrical value is floating then that will give one determined value when tested electrically in a determined way – in a semiconductor circuit the test is always either if the bit can supply current to ground or to the positive rail and the answer for a floating line is ‘no’ both ways. The logic circuit has been damaged so that it is different from the way it was designed but it is still a logic circuit which responds to given inputs with given outputs, in this hypothetical case producing a floating bit in some conditions. The functionality depends on the circuit around the damaged area and it may be more complicated input to output than always on or always off, but it should be deterministic.

The situation may be encapsulated as hidden deterministic hardware aliasing, axiomatised as follows with respect to the addresses produced by sequences of processor operations:

Axioms

1. A machine code copy instruction copies the physical bit sequence exactly, such that a copied address accesses the same memory location as the original;
2. repeating the same sequence of operations produces an address that physically has exactly the same bit sequence and accesses the same location;
3. logically different addresses always have physically different bit sequences.

By ‘logically different’ is meant different in terms of the intended arithmetic. In the example, 4 and 5 are not logically different as they are equivalent in the equivalence relation with respect to which arithmetic is well-defined, with 4 \equiv 5, but 5 and 6 are logically different and 5 \not\equiv 6 in the equivalence relation. The 4 and 5 can be thought of as different physical encodings of the same logical number (here, 2), while 5 and 6 are different physical encodings of different logical numbers.

Axiom 1 (‘faithful copy’) implies a compiler can generate code that copies an address for later use after writing through it, and the copy can be trusted to retrieve the written value. The address must not be altered, not even by adding zero, as any arithmetic calculation at all potentially alters the physical representation of the address as a sequence of bits, which then fails to access the same memory location. In the example given, 0 is equivalent to 1, so adding what is arithmetically zero may in fact mean adding one in physical terms.

Axiom 2 (‘repeatability’) allows for some calculations on addresses, so long as they are repeated exactly each time. That is useful because machine code instructions to read or write a memory location generally take a base address a in a register and adds a displacement d embedded in the instruction to get effective address a+d for the access. It is impossible to avoid the processor doing that one addition, but it does not matter because the same calculation is repeated at each access, with physically the same sequence of bits resulting.

Axiom 3 (‘no confusion’) guarantees that the representations as physical sequences of bits of what are logically different addresses do not step on each other. The addresses with bit sequences 5 and 6 in the example represent logically different numbers (logically 2 and 3 respectively).

The layout of this paper is as follows. Section II explains how to compile to obtain code ‘safe against hardware-aliasing’ in the most general context. The generated code has to cope with variations in the addresses produced, while they are
actually governed by a ‘hidden determinism’, as described above. Section III details an extension in which variations are deliberately introduced by the compiler (which can cope with them) ‘to the maximal extent possible’ as described in in the section, and that is called chaotic compilation. The section finishes with an argument that unrolling code to a length that is exponential (super-polynomial) in the number of bits per word and then compiling it chaotically results in safety against polynomial complexity attacks aimed at determining what the data in the runtime trace means. The technique introduced in Section II can be seen as coping with apparently unreliable addressing (really deterministically generated) and the technique of Section III extends that to deterministically generate apparent unreliability in data in general, and cope.

II. Safe Compilation for Hardware Aliasing

The working principle for generating viable code in this kind of environment is that each address that is written should be saved for later read, as per Axiom 1 (‘faithful copy’) of Section I. The problem is that it is saved at an address, which must also be saved, and so on recursively. Axiom 2 (‘repeatability’) allows a backstop to be put on the recursion, via base addresses that are produced at compile time and a repeated calculation at runtime based on them. But no finite set of addresses can suffice for nested function calls to unbounded depth, so the runtime stack must be involved. The first problem is how to manipulate the stack pointer so addresses and other data might be saved and recovered reliably from stack.

A. Stack Pointer 101

The standard compiler-generated function call sequence decrements the stack pointer register \( sp \) by the amount that will be needed for local storage in the function immediately on entry to the function body, and increments it again before exit:

\[
\text{call to function} \\
\ldots \\
\text{function code start:} \\
\quad \text{decrement} \ sp \\
\ldots \\
\quad \text{increment} \ sp \\
\text{return}
\]

That does not work in a hardware aliasing environment, because the increment does not necessarily restore exactly the same physical representation originally in the stack pointer register. Instead, the caller gets back a possibly different set of bits that, however, means the same thing arithmetically. Being different, it references a different location in memory.

The frame pointer register \( fp \) must be co-opted to copy the stack pointer, and copy the stack pointer back from it just before return from the call:

\[
\text{function code start:} \\
\quad \text{copy} \ sp \text{ to } fp \\
\quad \text{decrement} \ sp \\
\quad \ldots \\
\quad \text{copy} \ fp \text{ to } sp \\
\text{return}
\]

That is the standard unoptimised function call sequence from a compiler but optimisation will replace it with the \( fp \)-less code (1). The GNU gcc compiler (for example) with -fno-omit-frame-pointer on the command line turns off optimisation and produces the code (2), which works with hardware aliasing.

\[
\text{function code start:} \\
\quad \text{save old } fp \text{ to } 1 \text{ below } sp \\
\quad \text{copy } sp \text{ to } fp \\
\quad \text{decrement } sp \\
\quad \ldots \\
\quad \text{copy } fp \text{ to } sp \\
\quad \text{restore old } fp \text{ from } 1 \text{ below } sp \\
\text{return}
\]

Saving below the caller’s stack pointer would ordinarily intrude on the callee’s stack area (‘frame’), so the decrement must be larger by one in order to leave room for it. As many as the compiler wants of the caller’s registers can be saved like this. The application binary interface (ABI) document for the platform specifies which registers the callee must save, and which the caller code must expect may be trampled on and must save itself. The frame pointer and stack pointer are callee-saving in (3).

The function call code (3) works well with hardware aliasing. It allows local variables for the function to be reliably addressed as \( sp+d \) on the stack, where \( d \) is a displacement between 0 and the function frame size. The \( d \) is supplied as an embedded constant in a load or store machine code instruction (see below in (4-5)) that references the stack pointer register, containing \( sp \), as the base for the displacement. The processor calculates \( sp+d \) for the effective address passed to memory.

B. Variables

With the function call sequence in (3), accessing local variables is simple. A word-sized local variable \( x \) is assigned a position \( n \) on the stack and the compiler issues a load instruction (\( lw \)) to read from there to register \( r \):

\[
\text{lw} \ r \ n(sp) \quad \# \text{load from offset } n \text{ from } sp \quad (4)
\]

The processor calculates \( sp+d \) but repeats the same calculation at every access, so by Axiom 2 of Section I the same sequence of bits for the address is produced every time, and it accesses the same spot in memory. To write the variable, a store instruction (\( sw \)) replaces the load instruction:

\[
\text{sw} \ n(sp) \ r \quad \# \text{store to offset } n \text{ from } sp \quad (5)
\]

For a global variable at an address \( a \) in (heap) memory, the compiler offsets from the zero register \( zer \) instead:

\[
\text{lw} \ r \ a(zer) \quad \# \text{load from address } a \quad (6)
\]

The zero register contains a fixed base value. The effective address sent to memory is \( a+0 \), which is possibly a physically different sequence of bits to \( a \) (representing the same value), but the calculation is repeated exactly each time so the same memory location is accessed each time.
Variables in the parent’s frame may also be accessed. If
the function is defined within another function, we shall call
it an interior function (‘nested is the standard term, but it
risks confusion with ‘nested’ function calls – one function
called from another). The compiler arranges that the exterior
function’s frame pointer is handed down at runtime in the c9
register (it is c9 in our own platform’s ABI; it may be different
in other ABIs) and that is preserved through successive interior
function calls. Then a load or store instruction using c9 instead
of sp or zer reliably accesses the exterior function’s variables
on the stack.

C. Arrays

Arrays present the real difficulties as entries are fundamentally
always accessed by address and addressing is fundamentally
unreliable in a hardware aliasing environment.

There are (at least) two common but different ways of
addressing the entries in an array a. That is (a) via a load
or store instruction with fixed displacement n from the array
address a (that is ‘a[n]’), or (b) via a pointer with value p
that ranges through the array starting at a and steps through
the elements until the desired one is reached, at which point a
load or store instruction with displacement 0 from the pointer
(‘p[0]’) is applied. Those two modes were considered in our
earlier work [8] (an anonymised version will be available from
the Chair), which continues to be the only work we know
of on how to even possibly get around hardware aliasing.
The two calculations (a) and (b) for the effective address are
respectively a + n and a + 1 + 1 + ... + 1 + 0. The calculations
may produce physically different sequences of bits to be sent
to memory, so the two are mutually incompatible and one or
the other must be used all the time for consistency. But both
have proven too restrictive in practice. It is as common, for
example, for real code to step a pointer down through an array
as to step up through it, and the transformation the compiler
needs to do results in prohibitively inefficient code at runtime.
Evidently also, there are many other ways of addressing array
entries commonly encountered in source code and we cannot
be expected to cater for them all.

We have accepted instead an engineering compromise in
which array access is not for general-purpose use going to
be constant time. For special purposes, one of the addressing
modes (a) and (b) may be used, but that would be liable to
cause programming mistakes at application-level. For arrays
of size N it turns out the compiler can provide access in
log N time in a simple manner that is safe and reliable for all
methods of calculating an index or pointer, known or unknown.

Linear complexity code will be presented first. To read
(local) array element a[n] the code tests n against each of
0, ..., N−1 in turn and chooses one address for each entry:

\[
\begin{align*}
(n == 0)?a[0]: \\
(n == 1)?a[1]: \\
\cdots
\end{align*}
\]

(7)
The equality tests are arithmetic and are therefore insensitive
to the physical representation of the value n of N as possibly
physically different sequences of bits. The generated machine
code always passes effective address a + d to memory where
d is the displacement from the base of the array for the entry
and a is the address sp + k, where k is the position on the
stack allocated by the compiler for the lowest array element
a[0]. The code is just the one machine instruction:

\[
\begin{align*}
\text{lw } r d(r) & \quad \# \text{ load from address } a+d \\
& \quad \# \text{ with } a \text{ in } r \text{ to } r
\end{align*}
\]

(8)
The address a is supplied by a preceding instruction:

\[
\begin{align*}
\text{addi } r s p \quad & \quad \# \text{ add } k \text{ to } s p \text{ in } r \\
\text{lw } r d(r) & \quad \# \text{ load from address } a+d
\end{align*}
\]

(9)

That produces the same calculation sp+k for a every time.

Improving this code to log N complexity means using a
binary tree instead of linear lookup for the value n of N,
deciding first if n is below N/2 or above it, then on what side
of N/4 or 3N/4 it is, and so on. Code for writing instead of
reading follows the same pattern, with store instead of load
instructions at the leaves of the binary tree or linear sequence.

The same form works for pointer p accesses, provided the
compiler knows what zone of memory it points into. We have
tightened the type system of C (the source language for our
prototype compiler) so the pointer is declared with the name
of a (possibly over-large) array a into which the programmer
guarantees it points at runtime:

\[
\text{int } *p \text{ restrict } a
\]

(10)

That selects array a as the target zone for p.

Some porting has to be done for existing code, marking out
areas into which different pointers point. It generally turns out
to mean declaring a global array from which objects of the
kind pointed to are allocated from, or declaring one function
as interior to another function (for example, main) where the
target zone of the pointer is declared as local on the stack.

A restrict pointer type is narrower than it would otherwise
be but there are no no semantic changes to the language
so the programmer does not have to relearn anything. The
programmer does (usually) have to make changes, but the new
code is valid in unmodified C, so it can be checked. Ideally it
is obtained via a sequence of careful code transformations. The
conservative choice is usually to replace ad-hoc declarations
with calls to an object factory for each compound type.

The following code is suitable for lookup via pointer p:

\[
\begin{align*}
(p == a+0)?a[0]: \\
(p == a+1)?a[1]: \\
\cdots
\end{align*}
\]

(11)

It is insensitive to the way the pointer p is calculated because
the equality tests are arithmetic and are not derailed by the
aliasing in memory addressing. A selection a[d] is made, and
the same lookup code (8) for a[d] is executed each time, giving
the same result.

This code can (also) be made log N complexity with a
binary tree structure. It can be converted for write by replacing
load instructions at the leaves with store instructions.

These constructions make pointer-based addressing consist-
tent with access via an array index in the hardware aliasing
context. The idea is to make the choice of address arithmetically, and then reuse that same address or calculation for the address again and again.

If the number N of array elements is determined at runtime (the C '99 standard adds so-called variable length arrays), then a 'late binding' code pattern is needed instead. The following generated code generalises (11) to read reliably through pointer p for a number N of elements that is a local variable at runtime:

\[
\text{for (int } d=0; d<N; d++) \\
\text{ if (p == a+d) } \{ \text{return a[d]; } \} \quad (12)
\]

The effective address passed to memory is \( sp + k + (0 + 1 + \cdots + 1) + 0 \), where \( a = sp + k \) is the address of array \( a \), and the 1s are repeated \( d \) times to address the \( d \)th element of the array. This is not the same calculation as in (11) so it is not generally compatible with that in this kind of environment. The compiler must always generate either the form (11) or the form (12). If there are no dynamically sized arrays in the code then it can afford to use (11) (the generated code is longer but conceptually simpler). If there are dynamically sized arrays then it must use the form (12). Tighter distinctions may be possible, but we have not explored them.

The same form must be used for indexed read:

\[
\text{for (int } d=0; d<N; d++) \\
\text{ if (n == d) } \{ \text{return a[d]; } \} \quad (13)
\]

The calculation for the effective address passed to memory is the same as in (12). Both (12-13) can be modified for \( \log N \) complexity, and then the modified form must be used always.

Writes replace the ‘\( a[d] \)’ return (translated to a load machine code instruction by the compiler) with a ‘\( a[d] = x \)’ (translated to a store machine code instruction).

\textbf{D. Data Types}

We will not unduly belabour the topic here, but compound (and short) data types need special consideration, at least because compound data may contain arrays and arrays need special consideration (above). Indeed, a common programming style in C is to access the members of a compound data type as though the whole were an array of words, and to access the members via a pointer to word. Unless debugging memory pointer problems is a favourite pastime, the programmer wants the compiler to get both modes of access (conventional and as an array of words) right.

The trick for the compiler is always to treat records with named fields ('struct' in C) as word arrays and translate the field name to an array displacement. The declaration

\[
\text{struct \{ int } a; \text{ int } b; \} \ x
\]

declares \( x \) with two named fields, \( a \) and \( b \), each one word wide. It occupies two words on the stack at displacements \( k \) and \( k' \) (the value \( k+1 \)) respectively from the stack pointer. The compiler generates accesses to the fields \( x.a \) and \( x.b \) just as it would for any local variables situated there, by calling

\[
\text{lw } r \ k(\text{sp}) \quad \# \text{ load from } x.a
\]

to read from \( x.a \), for example. The effective address passed to memory is \( sp+k \). To access \( x.b \), the address passed is \( sp+k' \) instead. The compiler generates the code for array access explained in the section above, and source code that accesses the fields of the struct as though it were an array works too.

Long atomic types such as \texttt{double} are also treated as arrays of words by the compiler. But most platforms have double-word load and store instructions that will fetch/write two words at once:

\[
\text{ld } r \ k(\text{sp}) \quad \# \text{ double word load}
\]

and only the address of the first word is given to the instruction. Registers are indexed as pairs for this instruction, and the partner to \( r \) is loaded up by the instruction with the word at address \( k+1 \).

But that is not necessarily compatible with treating the double as a two-word array in a hardware aliasing environment. If the double is on the stack then the effective address for the first word is \( sp+k \), say. The processor may request a double-word from memory at that address. Or it may request two words, one at \( sp+k \) and one at \( (sp+k)+1 \). Both address calculations are reliably repeatable, according to the axioms of Section I, but by those axioms there is no guarantee that the latter calculation accesses the word at one beyond \( sp+k \) in memory. Indeed, the example given in that section shows that if \( sp+k \) gives one of the answers \{4, 5\}, then the arithmetic must be so arranged that \( (sp+k)+1 \) gives one of the answers \{6, 7\}. It may be that 4 is produced for the former, and 6 for the latter, and those are not consecutive positions in memory.

Overall, it is safer that the compiler not make use of double word instructions, though if the program contains no accesses to doubles as two-word arrays, then it is perfectly safe.

The difficulty remarked above with \texttt{double} transfers to accessing the individual bytes of a single word too. It is safer overall not to use the byte-oriented instructions that the platform provides, but to use arithmetic instead, as follows.

For index-oriented access to the characters of a string \( a \), the compiler generates code that splits the character index \( i \) into index \( d \) for a word consisting of a sequence of 4 characters, and offset \( j \) for the wanted character within the word:

\[
d = i/4; \\
j = i\%4;
\]

(17)

Then the character is obtained via an array-of-words lookup and the following arithmetic for the \( j \)th char of the \( d \)th word:

\[
(a[d] / 256^j) \% 256
\]

(18)

In our own prototype compiler, we have preferred to avoid the complication and pack characters only one to a word, at the cost of an inefficient use of memory.

\textbf{III. DELIBERATELY CHAOTIC COMPILATION}

We can take the general scheme for compiling around hardware aliasing on the platform and use it to work around variations introduced by the compiler itself. The point is that varying the object code tends to obscure what it does, and
obfuscation is a legitimate aim of some fields of software engineering. Many companies might like to distribute object code that is so obfuscated that it cannot be reverse engineered, while not being hampered in execution (of course it is easy to produce code that theoretically cannot be reverse engineered – it suffices to include a loop that in parallel to everything else that the program does, searches at low priority for an inconsistency proof for integer arithmetic, and if it finds one, interrupts the rest of the program, and nobody can say for certain if the program will complete normally or not – but in practice a skilled engineer can make a good job of it).

The aim in chaotic compilation is to compile the same source code differently each time, forming object codes that have the same overall functionality but the runtime traces vary to the maximal extent possible within these constraints:

1) The same sequence of machine code instructions executes, in the same order.
2) The constants embedded in each machine code instruction differ to the maximal extent possible.
3) The data written to registers and memory differs to the maximal extent possible.

The idea is to compile program $p_1$ and prepare data $d_1$ for it, and to compile program $p_2$ and prepare data $d_2$ for it. The two data sets represent the same thing, but their presentation for the two compiled programs differs. Then $p_1(d_1)$ and $p_2(d_2)$ are run. Comparing the two runtime traces, the characteristics 1)-3) above are seen. The ‘differs to the maximal extent possible’ refers to the stochastic distribution of outcomes. Compilation is randomised, so each runtime trace is one of a range of possible traces, and the ideal is that each trace is exactly as frequent an outcome as any other among the possibilities. That is a ‘flat’ distribution of outcomes, which is a maximal entropy\(^2\) distribution in information theoretic terms. That is, no bias or other tendency is discernible. Even though human programmers naturally tend to use low numbers like 0 and 1, the compiler will have randomised the object code so that tendency, and any other, is not present. So ‘differs to the maximal extent possible’ means a flat probability distribution of the stated observations, which is technically chaotic.

‘Getting the intended result’ would be a fourth constraint, but it is already said that the overall functionality is retained.

It will be argued that chaotic compilation may be applied to any program such that on a platform with a n-bit word: the compiler will issue the instruction with a displacement constant \(\Delta\) different from \(n\):

\[
\text{lw } r \Delta(s) \quad \# \text{ load offset } n \text{ from } sp
\]

\(\Delta\) is randomly chosen and the register \(s\) has been pre-set to contain \(sp + n - \Delta\), where \(sp\) is the nominal value of the stack pointer. The bit sequence passed to memory by (19) as effective address to read from is the result of the calculation:

\[
sp + n - \Delta + \Delta
\]

The compiler always emits the same instruction sequence, getting the same address always as result, but it has to ensure that the \(\Delta\) used in place of the \(n\) is the same each time, for each \(n\). So it maintains a vector \(\Delta\) indexed by stack location \(n\). (a similar vector \(\Delta_Z\) is maintained for the heap). Then the \(\Delta\) in (19) is really \(\Delta = \Delta n\) and the instruction in (19) is:

\[
\text{lw } r \Delta n(s) \quad \# \text{ load offset } n \text{ from } sp
\]

The vector \(\Delta\) is changed randomly by the compiler as it works through the source code and is a source of extra variation, but as explained above it seems not to do anything because the base address read from register \(s\) is asserted in (20) to be offset to compensate. That is not true. The compiler controls the offset in register \(s\) too, as explained below, so that random variations from nominal in every register and memory location are produced and accounted for. The essence is that:

\[\text{Each machine code instruction that writes is freely varied to the maximum extent possible.}\]

For example, the load instruction of (21) has one embedded constant \(\Delta n\) and it is freely varied by the compiler. The
instruction is exceptional, however, in that it writes, but not in any way that is controlled by the varied constant. The result always ends up in the named register \( r \). Instead ‘writes’ must be understood as ‘having an observable effect on the trace’.

B. Content Deltas

As remarked above, the stack pointer \( \text{sp} \) does not contain the value \( sp \) that it notionally should have but instead is offset from that by a randomly generated value \( \delta \). That is true of the content of every register and memory location at every point in the generated code. The compiler maintains a vector \( \delta \) of the offset delta for content in each register and memory location, varying it as it passes through the code, and the \( \delta \) for the stack pointer register is \( \delta = \delta \text{sp} \).

We need to work through enough detail of what the compiler does to show the principle (\( \text{ii} \)) is satisfied, but most will be omitted. The following is an abstract, declarative rendering of what the compiler does to translate a non-side-effecting expression \( e \) of the source language, which is the simplest part of its work.

Let the compiler be \( C_r[-] \), translating \( e \) to machine code \( mc \) that targets the result for register \( r \) at runtime. That is:

\[
(mc, \delta) = C_r[e]
\]  

(22)

Let the state of the runtime machine before \( mc \) runs be \( \sigma_0 \), let the nominal value for the expression\(^3\) be \( [e]^{\sigma_0} \), then running code \( mc \) takes state \( \sigma_0 \) to state \( \sigma_1 \) in which the value in register \( r \) is offset from the nominal value by the randomly generated amount \( \delta r \). That is:

\[
\sigma_0 ^{mc} \sigma_1 \text{ where } \sigma_1(r) = [e]^{\sigma_0 + \delta r}
\]  

(23)

Re-rendering the code in (21) to read the \( n \)th location on the stack and show explicitly the previous instruction that prep the base address (in register \( r \)) for the load:

\[
\text{addi } r \text{ sp } k \quad \# k = n - \delta \text{sp} - \Delta n
\]

\[
\text{lw } r \Delta n (r) \quad \# \text{read } n \text{th stack location}
\]  

(24)

The memory receives as effective address to read from the result of the following calculation:

\[
s p + \delta \text{sp} + k + \Delta n \text{ where } k = n - \delta \text{sp} - \Delta n
\]  

(25)

The stack pointer register \( \text{sp} \) contains the nominal value \( sp \) offset by \( \delta \text{sp} \). Summing, the address has the arithmetic value \( sp+n \). The physical representation as a sequence of bits may both be different from nominal and may vary, as discussed in Section I: one might equally get a 4 as a 5 from the calculation, following the example there. However, the calculation is the same every time so the bit sequence passed to memory is the same every time, by Axiom 2. It cannot hit the memory location associated with any other (logical) address by Axiom 3, and the calculation for the address (25) is repeated exactly at every access via (24) so it hits just one memory location of those feasible for the logical address.

The \( \delta \) and \( \Delta \) values are changed by the compiler at (just before) every point in the code where a write occurs. After the write the deltas for that location have to be maintained constant through the following sequences of reads from the same location along the code paths through that point, or the reads would miss. There are two instructions generated in (24) and both carry constants that can be varied by the compiler. However, the constraint on the right in (24) binds them and restricts the total variation possible. A further variation beyond that constraint would to vary the logical position \( n \) of the target on the stack at every write to it. That can be done but it is too tricky to describe here, so we will hypothesise that the position on the stack forms part of the intended program semantics and it cannot be varied.

Within that constraint, the two instructions in (24) can be varied maximally by the compiler, as required by (\( \text{ii} \)). It is just that, by virtue of the constraint, the entropy the compiler can introduce to the runtime trace via them is not \( 2 \times 32 \) bits (assuming a 32-bit word), but only \( 1 \times 32 \) bits. That is, if the \( \Delta n \) constant in the load instruction is freely chosen by the compiler, then the \( k \) constant in the preceding addition is determined by \( k = n - \delta \text{sp} - \Delta n \), and if the \( k \) constant is freely chosen then the \( \Delta n \) value is determined.

Closely related work presently under review [10] makes the above observations precise:

**Theorem 1.** The entropy in a trace over recompilations is the sum of the entropies of every instruction that writes that appears in it, counted once each.

The entropy of the two instructions combined in (24) is 32 bits (on a 32-bit platform). That can be seen as 32 bits for the first instruction, and zero for the second, as its variation is already determined once the first has been seen.

The compiler’s job in the chaotic compilation context is to do everything it can to maximise entropy in the trace. It turns out that following (\( \text{ii} \)) as a compiler design principle does that, which is why we have been careful to check for it above:

**Theorem 2.** The trace entropy is maximised when the compiler varies every instruction that writes to the maximal extent possible from recompilation to recompilation.

Successfully varying each instruction to the maximal extent possible provides a stochastic setting at runtime in which an observer cannot be sure what the numerical value of the data in the trace is really intended to mean even in terms of a statistical tendency, because the maximum 32 bits (on a 32-bit platform) of information caused to be written by the programmer at each point in the trace is swamped by that much contribution again from the compiler. But there are limits on what the compiler can do in terms of variation, as argued for (24) above.

But the constraint for (24) can be removed via a modification to the underlying platform. The idea is to allow potentially any address to stand for ‘the \( n \)th location on the stack’. That requires an extra hardware or software address translation unit

\(^3\)The ‘nominal value’ \( [e]^{\sigma} \) of expression \( e \) is is formalisable via a canonical construction: map a variable \( x \) in the expression to its register location \( r_x \) (the runtime value is offset by a delta \( \delta r_x \)), checking the content of \( r_x \) in the state and discounting the delta to get \( [e]^{\sigma} = \sigma(r_x) - \delta r_x \). Arithmetic in the expression is formalised recursively, with \( [e_1 + e_2]^{\sigma} = [e_1]^{\sigma} + [e_2]^{\sigma} \), etc.
between the runtime software process and memory. On being passed a new address \( a \) intended as the \( n \)th stack position, it remaps it to the next free address \( b \) in a previously designated contiguous linear region of memory \( R \), say the region between 1GB and 1.25GB, and memoizes the choice so the next time the address \( a \) is passed to it, it is mapped to \( b \) in \( R \) again. That gives each process access to 250MB, though the addresses \( a \) it generates range randomly across the full 32-bit range (0 to 4GB). The compiler inserts instructions in the object code that remove defunct mappings, keeping the memory needed down.

That unit exists and is part of every processor. It is the ‘translation lookaside buffer’ (TLB), and its job is to remap memory address space a page (8KB) at a time, but we need it to work with individual addresses, not whole pages. An easy solution is to simulate it in an underlying software layer. Given that, the compiler is free to vary \( n \) in (24) and the constraint in (25) relates three constants, \( k, n \) and \( \Delta n \), allowing for \( 2 \times 32 \) bits of entropy for the two ‘instructions that write’ in (24), satisfying (\( \Box \)) and allowing Theorem 2 to conclude the trace has been randomised (‘trace entropy is maximised’).

But there are still other constraints on compiler-induced variation due to computational semantics. The inputs and outputs of a copy instruction are the same, so the variations in them are the same and not independent. Also, the compiler must set the same variations from nominal values at the end of a loop as at the beginning, because it cannot tell in general how many times a loop will be traversed at runtime and must prepare the code for another traversal after one time through.

We will not go through all the code constructs, just loops, to show how and when the principle (\( \Box \)) must sometimes fail.

C. Loops

Let the statement compiler \( C[-] \) produce code \( mc \) from statement \( s \) of the source language, changing the combined database \( D = (\Delta, \delta) \) of offsets to \( D^s \) in the process. The offsets \( \delta \) are the intended variations from nominal values at runtime for the data content of each register and memory location and the offsets \( \Delta \) are the extra displacements for addressing described in Section III-A.

For legibility, pairs \((D, x)\) will be written \( D : x \) here. Then the statement above of what the compiler does with statements \( s \) is formalised as:

\[
D^s : mc = C[D : s] \tag{26}
\]

The notation emphasises the compiler is side-effecting on \( D \).

Compiling while \( e \) is means emitting code \( mc \) constructed from \( mc_e \) for \( e \) and \( mc_s \) for \( s \), with this shape:

\[
\text{start: } mc_e \quad \# \text{compute } e \text{ in } r \\
\text{beqz } r \text{ end} \quad \# \text{goto to end if } r \text{ zero} \\
\text{mc}_s \quad \# \text{compute } s \tag{27} \\
\text{b start} \quad \# \text{goto start} \\
\text{end:}
\]

That does not work as-is, because the code does not at the end of the loop reestablish the deltas that prevailed at loop start, so a second time through at runtime, much goes wrong. Extra code is needed after \( mc_s \), so-called ‘trailer’ instructions.

A trailer instruction adjusts the content of register \( r \) back to the delta \( \delta r \) off nominal at the beginning of the loop, starting from a delta \( \delta^s r \) at the end of the loop. It is as follows:

\[
\text{addi } r r k \quad \# \text{where } k = \delta r - \delta^s r \tag{28}
\]

Just the one instruction is required per register.

Trailer instructions that restore the \( n \)th stack location offset must also restore the address displacement constant used in load and store. That is a more complex code sequence:

\[
\begin{align*}
\text{addi } t0 & \text{ sp } j \quad \# j = n - \delta \text{ sp} - \Delta^s n \\
\text{lw} & t0 \Delta^s n (t0) \quad \# \text{load } n\text{th stack location} \\
\text{addi} & t0 t0 k \quad \# \text{modify by } k = \delta n - \delta^s n \\
\text{addi} & t1 \text{ sp } l \quad \# l = n - \delta \text{ sp} - \Delta n \\
\text{sw} & \Delta n (t1) t0 \quad \# \text{store } n\text{th stack location}
\end{align*}
\tag{29}
\]

(the \( t0, t1 \) registers are ‘temporary’ workspace). The first two instructions are the read stack code of (24), and the last two are the corresponding write code. In-between, the instruction (28) changes the content delta. The sequence reads with one address displacement, and writes with another, changing the location of the (changed) content.

The trailer sequences (28-29) introduce no entropy at all into the runtime trace and therefore fail the principle (\( \Box \)) (effectively, per instruction that writes, 32 bits of variation is needed from the compiler to mask programmer information). The constants in the instructions are determined by choices of deltas by the compiler for earlier instructions and it is impossible to execute the trailer instructions without traversing the loop body, which will execute those earlier instructions, so these trailer instructions are always ‘old news’ when they run.

The content of the registers or memory locations they affect during execution is correlated with the content of registers and memory locations at the start of the loop.

Other places where the compiler must put trailer instructions like (28-29) are where conditional branches join again, the labelled targets of \( \text{goto} \)'s, and at \text{return} from functions. Calls of interior functions also require ‘trailers’, but before the call, because the delta offsets in force at the point where the function was defined must be reestablished (that is a ‘come from’ semantics; c.f. \text{goto}). If there are global variables, then the same goes for ordinary (i.e., not ‘interior’ but top-level) function calls with respect to those globals they access.

At each of those points the principle (\( \Box \)) fails, because every instruction that writes (on a 32-bit platform) does not introduce 32 bits of entropy from the compiler.

D. The Argument for (\( \Box \))

Given the analysis above, the argument for (\( \Box \)) requires a program to be unrolled far enough before chaotic compilation so none of the points where (\( \Box \)) fails will be encountered in practice by an observer. Then by Theorem 1 the entropy in the observed part of the trace is sufficient to mask completely any input from the programmer, and an observer cannot say with any significant probability of being right (as the word length \( n \) tends to infinity) what any bit of data picked out of the trace means. A fuller sketch of the argument is as follows:
Proof: [Sketch for (O)] Suppose for contradiction that the
observer has a polynomial time method \( f(n,T) \) of working out
what the data beneath the encryption is at some \( m \) points
of interest in the trace \( T \) of program \( P \), where \( n \) is the platform
word size. For brevity assume \( P \) includes its intended inputs,
compiled-in. The observer sees runtime trace \( T \).

WLOG take \( m=1 \) and suppose the observer is interested in
only one particular bit in that particular register or location
in memory at that point, say the least significant bit \( b \). It is
last written to in the \( M \)th step of the trace before the point
of interest. Then the observer’s prediction \( f(n,T) \) is 0 or 1. Suppose also the program has been written in the
machine code subset consisting of addition instructions with
semantics \( x \leftarrow y+k \) (\texttt{addi } \( x\ y\ k \)) for a constant \( k \) embedded
in the instruction, and branch instructions with semantics
if \( x<y+k \) \texttt{goto } \( L \) (\texttt{blt } \( x\ y\ k\ L \)) for constant \( k \) and target
address \( L \) embedded in the instruction. (Those are enough
for computable functions, i.e., ‘programs’; c.f., the programming
language Fractran [11].)

A challenger reads a sequence of maximal entropy compi-
lations \( C[P_n] \) of \( P \) with the \( n \)-th being for a \( n \)-bit platform
as target, and \( P \) having been partially or completely unrolled
as \( P_{n'} \) with no loops or branches in the first \( 2^n \) (i.e., super-
polynomially many) machine code instructions. If the program
predictably ends before then, it is to be unrolled completely.
These are compilations of the same program \( P \) all with the
same end-to-end semantics that could be produced entirely
automatically (the constants in \( P \) can be expressed exactly
in the \( n \) bit words available on the platform, for all \( n \) considered).
The observer is invited to apply their method \( f \) and predict
the chosen bit \( b \) in the traces \( T_n \). By hypothesis, \( f(n,T_n) \) is
correct with probability at least \( B \) with \( B > 1/2 \) as \( n \to \infty \).

Let \( N \) be such that for \( n \geq N \) the word of interest for
the observer in the trace is produced by the unrolled part,
that is, \( 2^N \geq M \). Consider the program \( Q \) that is \( P_N \) with
the instruction that produces the word of interest changed from
\( x \leftarrow y+k \) to \( x' \leftarrow y+k' \) where \( k' = k+1 \), so the word is written
in \( Q \) to 1 more than in \( P_N \). But also all instructions in \( P_N \) that
read that register or memory location \( x \) before it is written over
again are changed in \( Q \) to semantically equivalent ones. That is,
an instruction \( z \leftarrow x+k_1 \) in \( P_N \) is changed to \( z \leftarrow x+k'_1 \) in \( Q \), where \( k'_1 = k_1-1 \); an instruction if \( x<z+k_2 \) \texttt{goto } \( L \) in \( P_N \) is changed to
if \( x<z+k'_2 \) \texttt{goto } \( L \) in \( Q \), where \( k'_2 = k_2-1 \). (There are only
a finite number of instructions to change, as \( P_N \) is finite, but
they may appear infinitely many times in the trace.)

Then the trace of \( Q \) is the same as the trace of \( P_N \) (and \( P_{n'} \),
for \( n \geq N \) except for that one word and its least significant
bit. Moreover, the traces from the code \( C[Q] \) are each of
them traces that may have been produced from code \( C[P_N] \) and/or
any \( P_n \) for \( n \geq N \) since the change from \( P_N \) to \( Q \) is one
that the compiler may make, i.e. \( Q = C[P_N] \) is possible.

Then the method \( f(n,-) \) applied to a trace of \( C[Q] \) on a
platform with an \( n \) bit word produces the same result as when
applied to a trace of \( C[P_N] \) (and \( C[P_n] \) for \( n \geq N \)), and so
must produce the right result for \( P \) with probability at least
\( B > 1/2 \) for \( n \) large enough. But that is the wrong result for
\( Q \). So the method \( f(n,-) \) produces the right result for \( Q \) with
probability \( 1-B < 1/2 \) for large enough \( n \), contradicting
the hypothesis, so the hypothetical method \( f \) does not exist.\( \Box \)

The result for \( m \geq 1 \) follows because if the observer had a
method \( f \) that made predictions at \( m \geq 1 \) points in the trace,
then the method \( g \) that throws away the \( m-1 \) predictions of
\( f \)’s at unwanted points would work as a method for \( m=1 \),
and the proof rules that out. Similarly for more than one bit.

The argument is not deep, as the empty program case shows,
but it is hard to codify and should increase understanding of
this area. The chaotic compiler constructions are reminiscent
of Yao’s garbled circuits [12], at \( n \) bits and with recursion.

IV. Implementation

A prototype C compiler \url{http://sf.net/p/obfusc} covers ANSI C
and GNU C extensions, including statements-as-expressions
and expressions-as-statements, gotos, arrays, pointers, structs,
unions, floating point, double integer and floating point data.
It is missing \texttt{longjmp} and efficient strings (\texttt{char} and \texttt{short}
is the same size as \texttt{int}). It is intended for use in encrypted
computing [13], [14], [15], [16], [17], [18], an emerging processor
technology in which inputs, outputs, and all intermediate
values in registers and memory are in encrypted form. Because
good encryption is one-to-many, and addresses are data like
any other, many physically different bit sequences (the ‘cipher-
text’) represent the address intended by the programmer (the
‘plaintext’), and platforms exhibit hardware aliasing at every
memory access, providing a testbed for theory and practice.

<table>
<thead>
<tr>
<th>PC</th>
<th>instruction</th>
<th>trace updates</th>
</tr>
</thead>
<tbody>
<tr>
<td>...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>35</td>
<td>addi t0 a0</td>
<td>-86921031</td>
</tr>
<tr>
<td>36</td>
<td>addi t1 zer</td>
<td>-327157853</td>
</tr>
<tr>
<td>37</td>
<td>beqz t0 t1</td>
<td>2</td>
</tr>
<tr>
<td>38</td>
<td>addi t0 zer</td>
<td>-1242455113</td>
</tr>
<tr>
<td>39</td>
<td>b 1</td>
<td></td>
</tr>
<tr>
<td>41</td>
<td>addi t1 zer</td>
<td>-1902505258</td>
</tr>
<tr>
<td>42</td>
<td>xor t0 t0 t1</td>
<td>-1734761313</td>
</tr>
<tr>
<td>43</td>
<td>beqz t0 9</td>
<td>-1734761313</td>
</tr>
<tr>
<td>53</td>
<td>addi sp sp</td>
<td>800875856</td>
</tr>
<tr>
<td>54</td>
<td>addi t0 a1</td>
<td>-915514235</td>
</tr>
<tr>
<td>55</td>
<td>addi t1 zer</td>
<td>-1175411995</td>
</tr>
<tr>
<td>56</td>
<td>beq t0 t1 2</td>
<td>259897760</td>
</tr>
<tr>
<td>57</td>
<td>addi t0 a0</td>
<td>111611509</td>
</tr>
</tbody>
</table>
A trace of the Ackermann function \(^4\) \(^5\)[19] compiled by the compiler is shown in Table I. The Ackermann function is the most computationally complex function possible, increasing in degree of complexity required to calculate it (polynomial, exponential, super-exponential, etc.) with each increment of the degree of complexity required to calculate it. The technique is extended to also generate as well as compensate for random displacements in the addressing, and extended again to generate and compensate for random displacements in the data content of all registers and memory (called chaotic compilation). A sketch proof is included to show this technique results in object code where it is difficult to discover the programmer’s intention at any points of the runtime trace, while maintaining the semantics. I.e., the compiled code is technically ‘obfuscated’.

### REFERENCES


---

**TABLE II**

<table>
<thead>
<tr>
<th>PC</th>
<th>instruction</th>
<th>trace updates</th>
<th>extra bits</th>
</tr>
</thead>
<tbody>
<tr>
<td>...</td>
<td>22340</td>
<td>addi t1 sp -418452205</td>
<td>t1 ← -877254954</td>
</tr>
<tr>
<td>22360</td>
<td>bne t0 t1 84</td>
<td>22394</td>
<td>addi t1 sp -407791003</td>
</tr>
<tr>
<td>22400</td>
<td>lw t0 86593746(t1)</td>
<td>t0 ← -865937451</td>
<td>1800719299</td>
</tr>
<tr>
<td>22424</td>
<td>addi t0 t0 -1668656853</td>
<td>t0 ← 1759716698</td>
<td>1081155516</td>
</tr>
<tr>
<td>22444</td>
<td>b 540</td>
<td>22488</td>
<td>addi t1 zer 1759716697</td>
</tr>
<tr>
<td>23008</td>
<td>bne t0 t1 44</td>
<td>23128</td>
<td>addi t0 sp -1763598776</td>
</tr>
<tr>
<td>23148</td>
<td>lw t0 -2072656779(r0)</td>
<td>t0 ← 2072656779</td>
<td>-1773201679</td>
</tr>
<tr>
<td>23168</td>
<td>addi t0 t0 1723413350</td>
<td>t0 ← -498991477</td>
<td>-981581771</td>
</tr>
<tr>
<td>23188</td>
<td>addi t0 t0 -1862832992</td>
<td>t0 ← 1331431371</td>
<td>-1629507929</td>
</tr>
<tr>
<td>23208</td>
<td>addi v0 t0 -1933143130</td>
<td>v0 ← ?</td>
<td>1680837379</td>
</tr>
</tbody>
</table>
| 23272 | jr ra | STOP | See Table I for Legend.

---

\(^4\)Initial and final content offset deltas are set to zero here, for readability.

\(^5\)Ackermann C code: int A(int m, int n) { if (m == 0) return n+1; if (n == 0) return A(m-1, 1); return A(m-1, A(m, n-1)); }.

\(^6\)Sieve C code: int S(int n) { int a[N]=0; if (n <= N-1) { for (int j=2; j<=n; ++j) a[j]=0; } for (int i=2; i<=n; ++i) { if (a[i]) continue; for (int j=i2; j<=n; +=i) a[j]=0; } if (a[i]) return i; return 0; }. 

**earlier calculations exactly. The technique is extended to also**


This paper has described the compilation of imperative source code for a platform that has hardware aliasing with hidden determinism. The technique depends on the compiler controlling the address displacement and address base for load and store instructions so that they are always the same for repeat accesses to the same memory location. That uses saved copies or repeats