SMT Encoding of Hybrid Systems in dReal*

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Abstract

Analysis problems of hybrid systems, involving nonlinear real functions and ordinary differential equations, can be reduced to SMT (satisfiability modulo theories) problems over the real numbers. The dReal solver can automatically check the satisfiability of such SMT formulas up to a given precision $\delta > 0$. This paper explains how bounded model checking problems of hybrid systems are encoded in dReal. In particular, a novel SMT syntax of dReal enables to effectively represent networks of hybrid systems in a modular way. We illustrate SMT encoding in dReal with simple nonlinear hybrid systems.

1 Introduction

An SMT (satisfiability modulo theories) problem is to check the satisfiability of first-order formulas with respect to certain decidable logical theories. Recently, SMT-based techniques, such as [4, 5, 6, 9], have been proposed to automatically analyze a general class of hybrid systems. One advantage of this approach is that we can apply existing state-of-the-art SMT techniques and tools, which are proven to be effective for analyzing discrete systems. Moreover, it is fairly easy to combine different numerical algorithms and decision procedures to analyze the continuous behavior of hybrid systems.

In SMT-based approaches, formal analysis problems of hybrid systems are encoded as SMT formulas. Since hybrid systems usually involve nonlinear real functions and ordinary differential equations (ODEs), the satisfaction problems of these formulas are in general undecidable. But if we take into account robustness properties under numerical perturbations, such problems become decidable up to an arbitrary precision $\delta > 0$ [7, 9]. Suppose that $\delta > 0$, provided by the user, is the bound on numerical errors that is tolerable in the analysis. A $\delta$-complete decision procedure for an SMT formula $\phi$ returns false if $\phi$ is unsatisfiable, and returns true if its syntactic numerical perturbation of $\phi$ by bound $\delta$ is satisfiable. This is practically very useful since it is not possible to sample exact values of physical parameters in reality.

The dReal tool [8] is an SMT solver to check the satisfiability of logic formulas over the real numbers up to a given precision $\delta > 0$ using $\delta$-complete decision procedures, involving various non-linear real functions, such as polynomials, exponentiation, trigonometric functions, and solutions of Lipschitz-continuous ordinary differential equations (ODEs). dReal is built on

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several existing packages to combine SMT and numerical techniques: opensmt [3] for general SMT decision procedures, realpaver [10] for the interval constraint propagation (ICP), and CAPD [1] for computing interval-enclosures of ODEs.

This paper shows SMT encoding for formal analysis of hybrid systems in dReal. To generate such SMT formulas from hybrid system specifications, dReal provide a front-end, called dReach [12], and the user need not know the details of SMT encoding in practice. A number of benchmarks and examples in this paper are available at http://dreal.github.io.

2 Background: Hybrid Automata

In this paper we use hybrid automata [11] as formal models of hybrid systems. Discrete states of a hybrid automaton $H$ are given by a set of control modes $Q$. Physical states of $H$ are given by a finite set $X = \{x_1, \ldots, x_n\}$ of real-numbered variables. A combined state of $H$ is then a pair $(q, \vec{v})$ of a mode $q \in Q$ and a vector $\vec{v}$ of real numbers. Each mode $q$ has an invariant condition, denoted by predicate $\text{inv}_q(\vec{x})$, that defines the set of all possible values of $X$ in mode $q$. Similarly, a set of initial states is expressed by using predicates $\text{init}_q(\vec{x})$. The continuous dynamics of a hybrid automaton $H$ is specified by a flow condition of the form $\frac{dx}{dt} = \text{flow}_q(\vec{x})$ for mode $q$, expressing a system of ordinary differential equations (ODEs) for the variables $X$.

A discrete transition between two modes $q$ and $q'$ is specified by a jump condition of the form $\text{jump}_{q,a,q'}(\vec{x}, \vec{x}')$, which can also be identified with action $a \in \Sigma$, given a set of actions $\Sigma$.

Example 1 (Periodic Water Tank). The water level in a tank is periodically controlled by its pump. For each period $T$, the pump is on if the water level is lower than $L_{\text{min}}$, and the pump is off if the water level is higher than $L_{\text{max}}$. The pump has two control modes $Q = \{m_{\text{on}}, m_{\text{off}}\}$ to denote its status. There are two real-numbered variables $X = \{x, \tau\}$ with $x$ for the water level and $\tau$ for its timer. Both modes have the invariant condition $\text{inv}(x, \tau) \equiv 0 \leq \tau \leq T$. Initially, the pump is on, $L_{\text{min}} < x < L_{\text{max}}$, and $\tau = 0$. The water level $x$ and the timer $\tau$ change according to the nonlinear flow conditions:

$$\frac{dx}{dt} = (p - a\sqrt{2g\sqrt{x}})/A \quad \text{if } q = m_{\text{on}}, \quad \frac{dx}{dt} = -a\sqrt{2g\sqrt{x}}/A \quad \text{if } q = m_{\text{off}},$$

where $A, p, a$ are constants determined by the size of the tank, the power of the pump, and the output of the tank. The jump conditions are given by:

- $\text{jump}_{m_{\text{on}}, a, m_{\text{on}}}(x, \tau, x', \tau') \equiv \tau = T \land x \leq L_{\text{max}} \land x' = x \land \tau' = 0$,
- $\text{jump}_{m_{\text{on}}, a, m_{\text{off}}}(x, \tau, x', \tau') \equiv \tau = T \land x > L_{\text{max}} \land x' = x \land \tau' = 0$,
- $\text{jump}_{m_{\text{off}}, a, m_{\text{on}}}(x, \tau, x', \tau') \equiv \tau = T \land x < L_{\text{min}} \land x' = x \land \tau' = 0$, and
- $\text{jump}_{m_{\text{off}}, a, m_{\text{off}}}(x, \tau, x', \tau') \equiv \tau = T \land x \geq L_{\text{min}} \land x' = x \land \tau' = 0$.

A hybrid system is often composed of a network of smaller hybrid systems, which is specified as a parallel composition of hybrid automata. For a parallel composition $H_1 \parallel H_2$ of two hybrid automata $H_1$ and $H_2$, its control mode is a pair $(q_1, q_2) \in Q_1 \times Q_2$ of $H_1$’s mode $q_1$ and $H_2$’s mode $q_2$. A physical state of $H_1 \parallel H_2$ is given by the set $X_1 \cup X_2$ of the real-numbered variables from both $H_1$ and $H_2$. For mode $(q_1, q_2)$, an invariant condition $\text{inv}_{(q_1, q_2)}(\vec{x}_1, \vec{x}_2)$ holds iff both $H_1$’s invariant condition $\text{inv}_{q_1}^1(\vec{x}_1)$ and $H_2$’s condition $\text{inv}_{q_2}^2(\vec{x}_2)$ hold. Likewise, an initial condition $\text{init}_{(q_1, q_2)}(\vec{x}_1, \vec{x}_2)$ holds iff both $\text{init}_{q_1}^1(\vec{x}_1)$ and $\text{init}_{q_2}^2(\vec{x}_2)$ hold.

The continuous interaction between $H_1$ and $H_2$ is modeled in their parallel composition $H_1 \parallel H_2$ by using shared variables $X_1 \cap X_2$, and their discrete communication is modeled by
using joint synchronous actions. A flow condition of mode \((q_1, q_2)\) is a system of ODEs for \(X_1 \cup X_2\) of the form \(\frac{dx_1}{dt} = \text{flow}^1_{q_1}(\vec{x}_1)\) \& \(\frac{dx_2}{dt} = \text{flow}^2_{q_2}(\vec{x}_2)\), where the flow condition of \(H_1\) in mode \(q_1\) is compatible with the flow condition of \(H_2\) in mode \(q_2\) for the shared variables \(X_1 \cap X_2\). For modes \((q_1, q_2)\) and \((q'_1, q'_2)\), a jump condition \(\text{jump}(q_1, q_2, a, q'_1, q'_2)(\vec{x}_1, \vec{x}_2, \vec{x}'_1, \vec{x}'_2)\) with action \(a \in \Sigma_1 \cup \Sigma_2\) holds iff for \(i = 1, 2\), either \(\text{jump}_{q_i, a, q'_i}(\vec{x}_i, \vec{x}'_i)\) holds when \(a\) is an action of \(H_i\), or \(q_i = q'_i\) and \(\vec{x}_i = \vec{x}'_i\) when \(a\) is not an action of \(H_i\). Notice that if \(a\) is a common action, then \(H_1\) and \(H_2\) must synchronize their transitions with action \(a\).

**Example 2** (Networked Water Tanks). Several water tanks in Example 1 are connected by pipes in sequence as shown in Figure 1 (adapted from [13, 14]). Every tank controller shares the same timer variable \(\tau\) with the flow condition \(\frac{d\tau}{dt} = 1\). That is, for tank \(i\), \(X_i = \{x_i, \tau\}\). The water level of each tank now depends on the levels of the adjacent tanks as well as the pump’s mode. Hence, the water level \(x_i\) of tank \(i\) changes according to the flow condition:

\[
\begin{align*}
\frac{dx_i}{dt} &= \left(p_i + a \sqrt{2g \sqrt{x_{i-1}} - a \sqrt{2g \sqrt{x_i}}}\right)/A_i \quad \text{if } q_i = m_{on}, \\
\frac{dx_i}{dt} &= \left(a \sqrt{2g \sqrt{x_{i-1}} - a \sqrt{2g \sqrt{x_i}}}\right)/A_i \quad \text{if } q_i = m_{off},
\end{align*}
\]

where \(A_i, p_i, a\) are determined by the size of the tank, the power of the pump, and the width of the pipe (\(x_0 = 0\) for the leftmost tank 1). Each water tank controller has the same period \(T \in \mathbb{R}\), and its jump conditions is labeled with the same action \(a\). Therefore, every controller synchronously performs its discrete transitions with the common action \(a\) according to the jump conditions in Example 1 (for each period \(T\), the pump is on if \(x_i \leq L_{\text{min}}\), and off if \(x_i > L_{\text{max}}\)).

### 3 SMT Encoding of Hybrid Automata

This section explains how bounded model checking problems of hybrid automata are encoded as SMT problems in dReal. The syntax of SMT formulas in dReal follows version 2 of the SMT-LIB standard [2] with extensions to declare systems of ordinary differential equations and their solutions. We illustrate such SMT encoding with the water tank examples. The dReach front-end [12] automatically generates such formulas from hybrid automata specifications.

**Variable Declarations.** For bounded model checking of a hybrid automaton \(H\) with depth \(N\), we need to encode its behavior for \(N\) steps of mode changes. A mode of \(H\) at the \(i\)-th step is expressed as a variable \(mode_i\). A variable \(time_i\) is declared to denote the time elapsed within \(mode_i\). For each state variable \(y \in X\), we use two sets of variables \(y_{i, 0}\) (0-variables) and \(y_{i, t}\) (t-variables) to denote the values of \(y\) at the beginning and the end of the \(i\)-th step, respectively. Such variables are introduced with the declare-fun keyword. For example, the two state variables \(x\) and \(\tau\) for the \(i\)-th step in Example 1 are declared as follows:

\[
\begin{align*}
(\text{declare-fun} \ mode_i () \ \text{Real}) \quad (\text{declare-fun} \ time_i () \ \text{Real}) \\
(\text{declare-fun} \ tau_{i, 0} () \ \text{Real}) \quad (\text{declare-fun} \ tau_{i, t} () \ \text{Real})
\end{align*}
\]
In dReal, we need that each real-numbered variable is bounded for δ-complete decision procedures. For variable \( y \), the `assert` statement

\[
\text{assert (and (\leq a y) (\leq y b))}
\]

declares its bound \( a \leq y \leq b \). For example, in Example 1:

\[
\text{assert (and (\leq 0 mode_i) (\leq mode_i 1) (\leq 0 time_i) (\leq time_i T) (\leq 0 x_i 0) (\leq x_i 0 10) (\leq x_i_t 10))}
\]

**Flow Declarations.** In order to declare systems of ODEs, dReal introduces the new keyword `define-ode`. A system of ODEs \( \frac{dx_1}{dt} = u_1, \ldots, \frac{dx_n}{dt} = u_n \) is defined by using the statement

\[
\text{define-ode flow ((= \frac{dx}{dt}[x_1] u_1) \ldots (= \frac{dx}{dt}[x_n] u_n))}
\]

with identifier `flow`. For example, the two nonlinear ODE systems in Example 1 are declared by:

\[
\text{(declare-fun x () Real) (declare-fun tau () Real) (define-ode flow_1 ((= \frac{dx}{dt}[x] (/ (- q (* (* a (sqrt (* 2 g))) (sqrt x))) A)) (= \frac{dx}{dt}[tau] 1)))}
\]

\[
\text{(define-ode flow_2 ((= \frac{dx}{dt}[x] (/ (* (* -a (sqrt (* 2 g))) (sqrt x))) A)) (= \frac{dx}{dt}[tau] 1)))}
\]

**Initial Conditions.** We define initial conditions as formulas on the initial mode variable `mode_0`, and the 0-variables to denote the values at the beginning of the initial step (that is, for variable \( y \), the variable \( y_0_0 \)). Such conditions are declared using `assert` statements in dReal. For Example 1, when mode `m_{on}` is denoted by number 0 and `m_{off}` is denoted by number 1:

\[
\text{assert (and (= mode_0 0) (= tau_0_0 0) (< L_{min} x_0_0) (< x_0_0 L_{max})))}
\]

**Jump Conditions.** SMT encoding of jump conditions is straightforward. Jump conditions are directly expressed as SMT formulas using `assert` statements and Boolean connectives. Since jumps happen at the end of each step, we define constraints between \( t \)-variables of the current step and 0-variables of the next step. For example, the jump conditions of the \( i \)-th step in Example 1 are written in dReal as follows, where \( j = i + 1 \):

\[
\text{assert (or (and (= mode_i 0) (= mode_j 0) (= tau_i T) (> x_i L_{max}) (= x_i 0 x_i_t) (= tau_j 0 0)) (and (= mode_i 0) (= mode_j 1) (= tau_i T) (> x_i L_{max}) (= x_j 0 x_i_t) (= tau_j 0 0)) (and (= mode_i 1) (= mode_j 0) (= tau_i T) (> x_i L_{min}) (= x_j 0 x_i_t) (= tau_j 0 0)) (and (= mode_i 1) (= mode_j 1) (= tau_i T) (> x_i L_{min}) (= x_j 0 x_i_t) (= tau_j 0 0)))}
\]

\(^1\) The `sqrt` function is Lipschitz continuous only if its domain is positive. The water level is always positive in our example. dReal reports an exception if the condition cannot be met.
Flow Conditions. Solutions of ODEs are expressed by using the new keyword integral in dReal. For example, an integral term \((y_0, \ldots, y_n) = (y_0, \ldots, y_n) + \int_0^t \text{flow}_i(t) \, dt\) is written as the statement \((\text{integral} \ 0 \ t \ [y_0, \ldots, y_n] \ \text{flow}_i)\), where \text{flow}_i\) is declared as a define-ode statement. For each \(i\)-th step, flow conditions are defined by constraints between 0-variables, \(t\)-variables, and time duration of the \(i\)-th step according to current modes. For the water tank example in Example 1, given 0-variables \([x_i^0, \tau_i^0]\) at the \(i\)-step, if the \(i\)-th step’s duration is \(\text{time}_i\), then the values of the \(t\)-variables \([x_i^1, \tau_i^1]\) are defined using integral statements according to its mode \(\text{mode}_i\), as follows:

\[
\begin{align*}
\text{assert} \ (\text{or} \ (\text{and} \ (= \text{mode}_i \ 0) \ (= \text{tau}_i \ [x_i \ t \ \text{time}_i] \ \text{flow}_1)) \ (\text{and} \ (= \text{mode}_i \ 1) \ (= \text{tau}_i \ [x_i \ t \ \text{time}_i] \ \text{flow}_2)))
\end{align*}
\]

Invariant Conditions. In a hybrid automaton \(H\), an invariant condition of mode \(q\) must be satisfied at any time as long as \(H\)’s current mode is \(q\). To encode invariant conditions, we need to deal with universally quantified formulas over time. Therefore, dReal introduce a new keyword \(\forall t\): the statement \((\forall t \ n \ [0 \ u] \ \phi(\vec{x}_t))\) declares that \(\phi(\vec{x}_t)\) holds for any time \(t \in [0, u]\) with the flow condition \text{flow}_n\) (that is, \(\forall t \in [0, u]. (\vec{x}_t = \vec{x}_0 + \int_0^t \text{flow}_n \, dt) \rightarrow \phi(\vec{x}_t))\). For example, the invariant condition \(0 \leq \tau \leq T\) for the \(i\)-step in Example 1 is written by the \(\forall t\) keyword as follows:

\[
\begin{align*}
\text{assert} \ (\text{and} \ (\forall t \ 1 \ [0 \ \text{time}_i] \ (\geq \text{tau}_i \ t \ 0) \ (\leq \text{tau}_i \ t \ T)) \ (\forall t \ 2 \ [0 \ \text{time}_i] \ (\geq \text{tau}_i \ t \ 0) \ (\leq \text{tau}_i \ t \ T)))
\end{align*}
\]

Bounded Model Checking. A safety requirement \(\phi\) of a hybrid automaton \(H\) is expressed using \(t\)-variables of the final step, and the reachability goal is given by its negation \(\neg \phi\). For Example 1, the requirement is that the water level \(x\) lies between \(L_{\min} - \epsilon\) and \(L_{\max} + \epsilon\) with a limit \(\epsilon > 0\) (that is, \(L_{\min} - \epsilon \leq x_N^i \leq L_{\max} + \epsilon\)). The reachability goal is given by its negation:

\[
\text{assert} \ (\text{or} \ (< x_N \ t \ (- L_{\min} \ \epsilon)) \ (> x_N \ t \ (+ L_{\max} \ \epsilon)))
\]

The entire formula for bounded model checking with depth \(N\) consists of: (i) variable and flow declarations, (ii) initial condition formulas, (iii) flow, jump, and invariant condition formulas for \(i = 0, \ldots, N\), and (iv) reachability goal formulas. It begins with the command \(\text{set-logic QF_NRA_ODE}\), and ends with the commands \(\text{check-sat} \ \text{exit}\). The bound \(N\) is iteratively increased from 0, and the verification is performed for every intermediate step.

If the SMT formula is satisfied, then we have a counterexample satisfying the reachability goal, and the safety requirement is violated. Otherwise, the safety requirement is satisfied since there is no counterexample. Because dReal uses \(\delta\)-complete decision procedures, the result is over-approximated by \(\delta\). A counterexample of \(\phi\) can violate \(\phi\) with numerical perturbation up to \(\delta > 0\) (i.e., a counterexample may be spurious). However, if no counterexample is found, then indeed there exists no counterexample regardless \(\delta\).

4 SMT Encoding of Compositions

A parallel composition of hybrid automata can be considered as a single hybrid automaton as mentioned in Section 2, and its bounded model checking problems can be encoded as SMT formulas in the exactly same way. However, the size of the formula can be very big. Consider
a parallel composition $H_1 \parallel \cdots \parallel H_n$ of $n$ hybrid automata $H_1, \ldots, H_n$. If each automaton $H_i$ has $k_i$ modes, then the size of the formula for $N$-step bounded model checking in the standard encoding is $O(N \cdot \prod_{i=1}^{n} k_i)$. This formula explosion problem can make SMT-based analysis of networks of hybrid systems practically infeasible.

One of the reasons is that the integral command only accepts complete ODE systems. In a parallel composition, each mode of a single automaton corresponds to a (partial) ODE system (where ODEs of some variables can be given in other automata), and a composited mode corresponds to a complete ODE system composed of those partial ODE systems.\(^2\) However, flow conditions cannot be decomposed in general, since variables in ODEs evolve simultaneously over continuous time (on the other hand, jump conditions of parallel compositions can be easily written in a compositional way according to the definition). For this reason, existing SMT techniques use the standard non-compositional encoding for networked hybrid automata.

We have recently introduced two new commands pintegral and connect in dReal to allow compositional encoding of networks of hybrid systems (and developed an SMT algorithm for the new syntax that will be presented elsewhere). Instead of declaring complete systems of ODEs as in Section 3, we only declare several partial systems of ODEs by using define-ode commands for parallel compositions of hybrid automata. For example, partial ODE systems for two connected water tanks in Example 2 are declared as the following five partial flow decorations:

```\[
\begin{align*}
(\text{define-ode } & \text{flow}_1) \\
(= & \frac{d}{dt} [\text{tau}] 1) \\
(\text{define-ode } & \text{flow}_2) \\
(= & \frac{d}{dt} [x1] (\text{/} (- q_1 (* (* a (sqrt (* 2 g))) (sqrt x1))) A_1))) \\
(\text{define-ode } & \text{flow}_3) \\
(= & \frac{d}{dt} [x1] (\text{/} (* -a (sqrt (* 2 g))) (sqrt x1)) A_1))) \\
(\text{define-ode } & \text{flow}_4) \\
(= & \frac{d}{dt} [x2] (\text{/} (+ q_2 (* (* a (sqrt (* 2 g))) (- (sqrt x1) (sqrt x2)))) A_2))) \\
(\text{define-ode } & \text{flow}_5) \\
(= & \frac{d}{dt} [x2] (\text{/} (* (* a (sqrt (* 2 g))) (- (sqrt x1) (sqrt x2))) A_2)))
\end{align*}
\]```

Then parameterized integral terms $\vec{y}_t = \vec{y}_0 + \int_t^0 [h_1(t), \ldots, h_k(t)] \, dt$ over flow parameters $h_1, \ldots, h_k$ are defined by using the keyword pintegral with the syntax:

```\[
(= [y_0 \ldots y_n \ldots t] \text{pintegral} 0 \text{t} [y_0 \ldots y_n \ldots 0] [\text{holder}_1 \ldots \text{holder}_k])
\]```

A concrete partial flow flow\_i is assigned to a flow parameter holder\_i using the keyword connect with the syntax `(\text{connect} holder\_i \text{flow\_i})`. Notice that “complete” assignments to such flow parameters $h_1, \ldots, h_k$ are supposed to give complete systems of ODEs.\(^3\)

For example, the $i$-step flow condition of the two connected water tanks in Example 2 includes only one parameterized integral term over three flow parameters holder\_a\_i for the timer, holder\_b\_i for tank 1, and holder\_c\_i for tank 2 (where $a_i = 3i + 1$, $b_i = 3i + 2$, and $c_i = 3i + 3$):

```\[
\begin{align*}
(\text{define-ode } & \text{flow}_1) \\
(= & \frac{d}{dt} [x1] \text{t} x2 \text{i} \text{t} \text{tau} \text{0} \text{t}) \\
(\text{define-ode } & \text{flow}_2) \\
(= & \frac{d}{dt} [x1] \text{i} \text{t} x2 \text{i} \text{0} \text{tau} \text{i} \text{0}) [\text{holder}_a \text{i} \text{holder}_b \text{i} \text{holder}_c \text{i})]
\end{align*}
\]```

After that, we separately assign partial flows to those flow parameters according to current modes using the connect keyword, where flow\_1 is for the timer $\tau$, flow\_2 and flow\_3 are for tank 1, and flow\_4 and flow\_5 are for tank 2:

\(^2\)For example, in Example 2, the water level $x_i$ of the $i$-th water tank depends on the water level $x_{i-1}$ of its input water tank, but the flow condition for $x_{i-1}$ is given in the automaton $H_{i-1}$, not in $H_i$.

\(^3\)The forall\_t command is not yet available for flows given by pintegral at the moment, but will be implemented soon.
Using this new encoding, the size of the formula for $N$-step bounded model checking can be $O(N \cdot \sum_{i=1}^{n} k_i)$ for a parallel composition $H_1 \parallel \cdots \parallel H_n$, when each automaton $H_i$ has $k_i$ modes (cf., $O(N \cdot \prod_{i=1}^{n} k_i)$ for the previous encoding). This can in turn greatly improve the performance of SMT-based analysis of networks of hybrid systems. For example, when we consider the two connected water tanks in Example 2, for bound $k = 3$, the new encoding can verify the system in 8 seconds, whereas the old encoding took 22688 seconds, provided that no other heuristics is applied (for details, see http://dreal.github.io/benchmarks/networks/water).

5 Concluding Remarks

We have illustrated SMT encoding for bounded model checking problems of hybrid systems in dReal. In this way, general hybrid systems involving nonlinear real functions and ordinary differential equations can be analyzed by dReal using $\delta$-complete decision procedures. A number of benchmarks and various examples (including the networked water tank example) are available at our tool website http://dreal.github.io. The dReach tool [12] provides a front-end of dReal to automatically generate SMT formulas from hybrid automata specifications. Since dReach currently only supports single hybrid automata, we plan to extend dReach to explicitly support networks of hybrid automata with compositional SMT encoding.

References
